

# 11<sup>th</sup> Russbach School on Nuclear Astrophysics

## Strongly r-process enhanced stars: constraining the pure r-process Ba/Eu abundance ratio from observations



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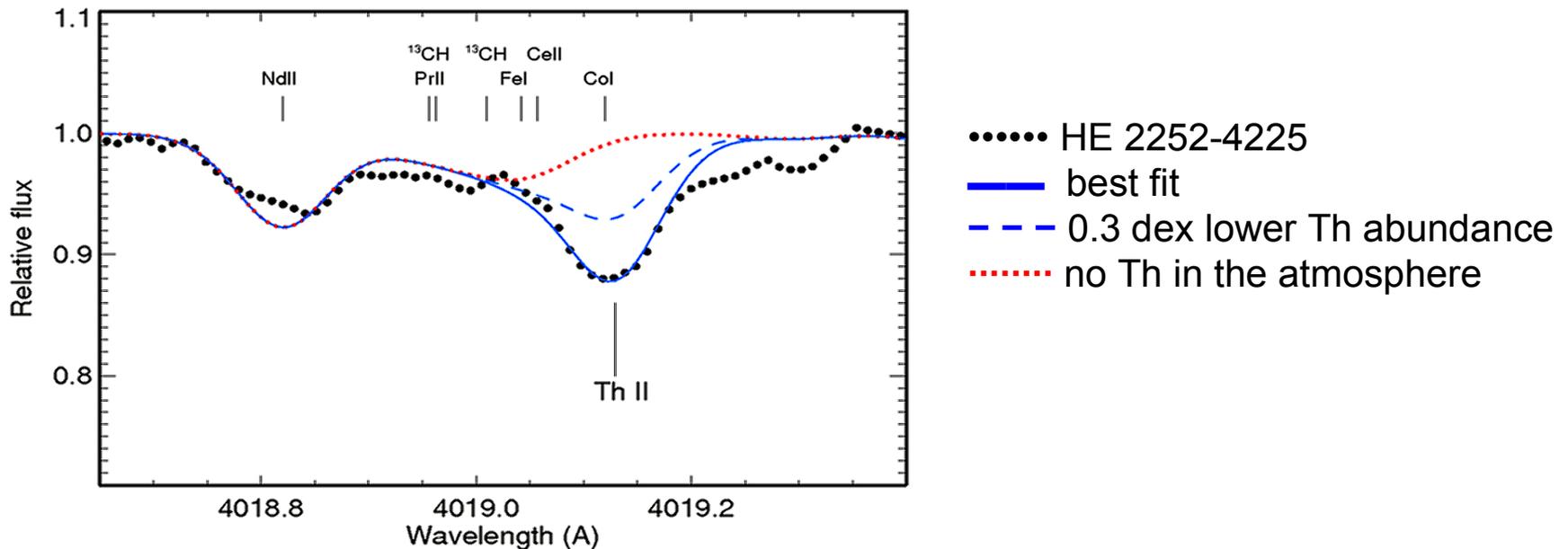
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March 10-14, 2014, Russbach, Austria

## Outline of this lecture

- ★ How to determine stellar chemical abundances?
  - Basics of stellar atmosphere and line formation modelling.
  - Uncertainties in derived abundances.
- ★ Ba and Eu abundances of r-II stars:
  - Why Ba/Eu?
  - Why r-II stars?
  - Observations vs. r-process models.

# Stellar element abundance is obtained from fitting theoretical spectra to observed spectral data



Observed spectrum should be of high resolution, high S/N ratio, wide wavelength coverage.

HE 2252-4225,  $V \approx 15^m$

It takes 9 hours to obtain 3400-6810 Å with

$R = \lambda/\Delta\lambda \approx 60\,000$ ,  $S/N \approx 100$

using 8-m telescope VLT (ESO, Chile), spectrograph UVES.

# Calculations of theoretical spectra

## Stellar atmosphere

Radiation escapes into space from thin layer on top of the stellar core.

Geometrically thin ( $H \sim 10^{-3} R$ ), but optically thick ( $\tau_{\nu} > 1$ ).

No generation of energy. Energy transport by radiation and convection.

## Step I: compute temperature and pressure stratifications.

Model atmosphere, assumptions:

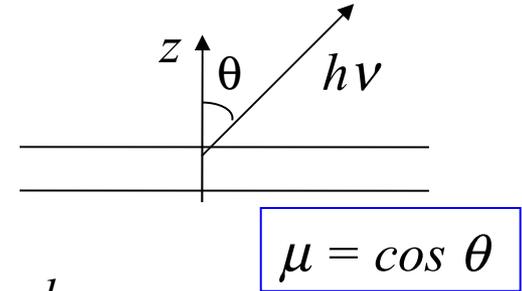
- ✓ composed of homogeneous layers (1D-geometry),
- ✓ static,
- ✓ in radiative and convective equilibrium.

Model atmosphere, parameters:

- effective temperature  $T_{\text{eff}}$ , measure of emergent flux,  $F = \sigma T^4$
- surface gravity  $\log g$ ,
- chemical composition,  $\{\epsilon_i\}$

## Step II: solve radiation transfer (RT) equation at line frequencies

$$\mu \frac{dI_\nu(z, \mu)}{dz} = -\chi_\nu(z) I_\nu(z, \mu) + \eta_\nu(z)$$



Opacity  $\chi_\nu = \chi_\nu^c + \chi_\nu^l$       emissivity  $\eta_\nu = \eta_\nu^c + \eta_\nu^l$

*Continuum opacity* : photoionization of H, He, metals, Rayleigh, Thomson scattering, etc.

*Line absorption:*  $\chi_\nu^l = \chi_\nu^l (n_{A,r,i}, \underbrace{f_{ij}, \gamma_R, \gamma_4, \gamma_6, HFS, IS}_{\text{Atomic parameters}})$

number density of absorbers

## Emissivity: how to compute?

- Local thermodynamic equilibrium (LTE)

(thermal processes):  $\eta_\nu / \chi_\nu = B_\nu(T)$

- non-LTE:

$$\eta_\nu^l / \chi_\nu^l = \frac{2h\nu_{ij}^3}{c^2} \frac{1}{\frac{n_i g_j}{n_j g_i} - 1}$$

How to compute  $n_{A,r,i}$  ?

- **LTE:**  $n_{A,r,i} = f(T, p)$  from the Saha-Boltzmann equations.

*LTE is invalid in line formation layers*

- mean free-path of photons is large,
- radiation field is far from TE.

- **Non-LTE:**  $n_{A,r,i}$  are determined from balance among radiative and collisional population and de-population processes.

**Statistical equilibrium (SE) equations:**  $dn_i/dt=0$

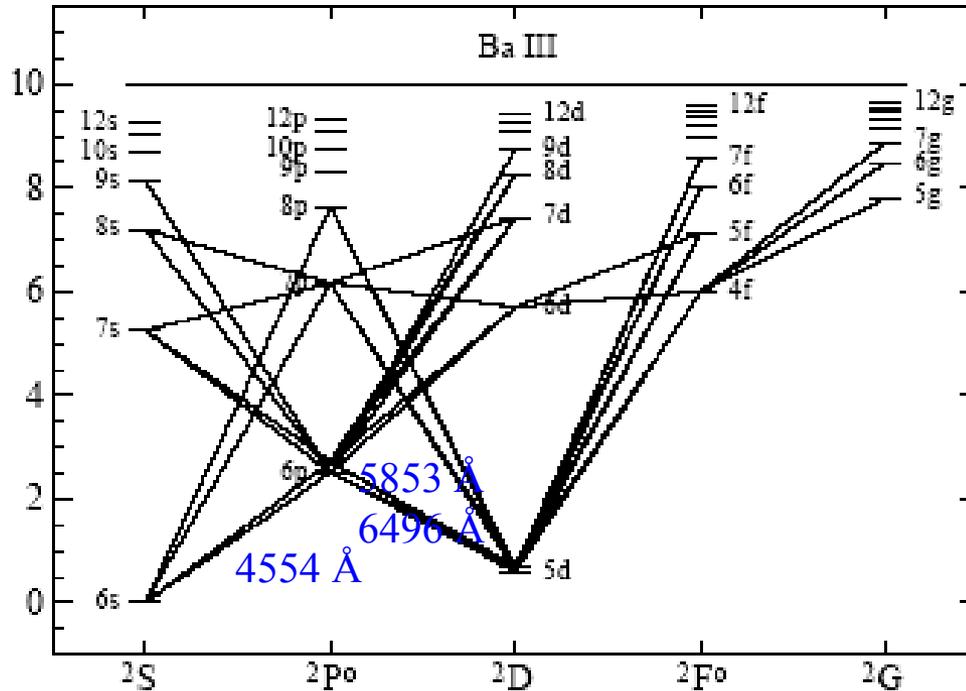
$$\left\{ \sum_{j \neq i} n_j (R_{ji} + C_{ji}) = n_i \sum_{j \neq i} (R_{ij} + C_{ij}) \right\} \quad i = 1, \dots, NL$$

+

$$\mu \frac{dI_\nu(z, \mu)}{dz} = -\chi_\nu(z) I_\nu(z, \mu) + \eta_\nu(z)$$

Solution of combined SE  
and RT equations

- Maxwellian velocity distribution,  $T_e = T_A = T_i$
- Real atomic term structure is represented by model atom.



Atomic term structure  
of Ba II

Excitation and ionization state of the matter at any depth point depends on physical conditions throughout the atmosphere.

$$n_i = f(n_1, \dots, n_{NL}, J_1, \dots, J_{NF})$$

Influence of departures from LTE  
on Ba abundances of  
CS 22892-052, 4800/1.5/-3.1

Mean abundance,  $\log \varepsilon = \log n_{\text{Ba}}/n_{\text{H}} + 12$

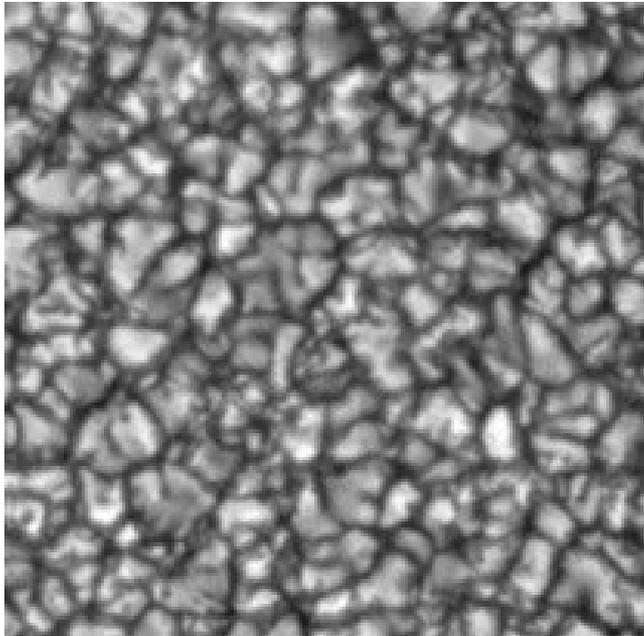
	LTE	non-LTE
Ba II 4554, 4934	$0.02 \pm 0.07$	$-0.18 \pm 0.01$
Ba II subordinate lines	$0.02 \pm 0.11$	$-0.15 \pm 0.02$

Note dramatic reduction of statistical error,  
when moving from LTE to non-LTE.

This favours non-LTE line formation for Ba II.

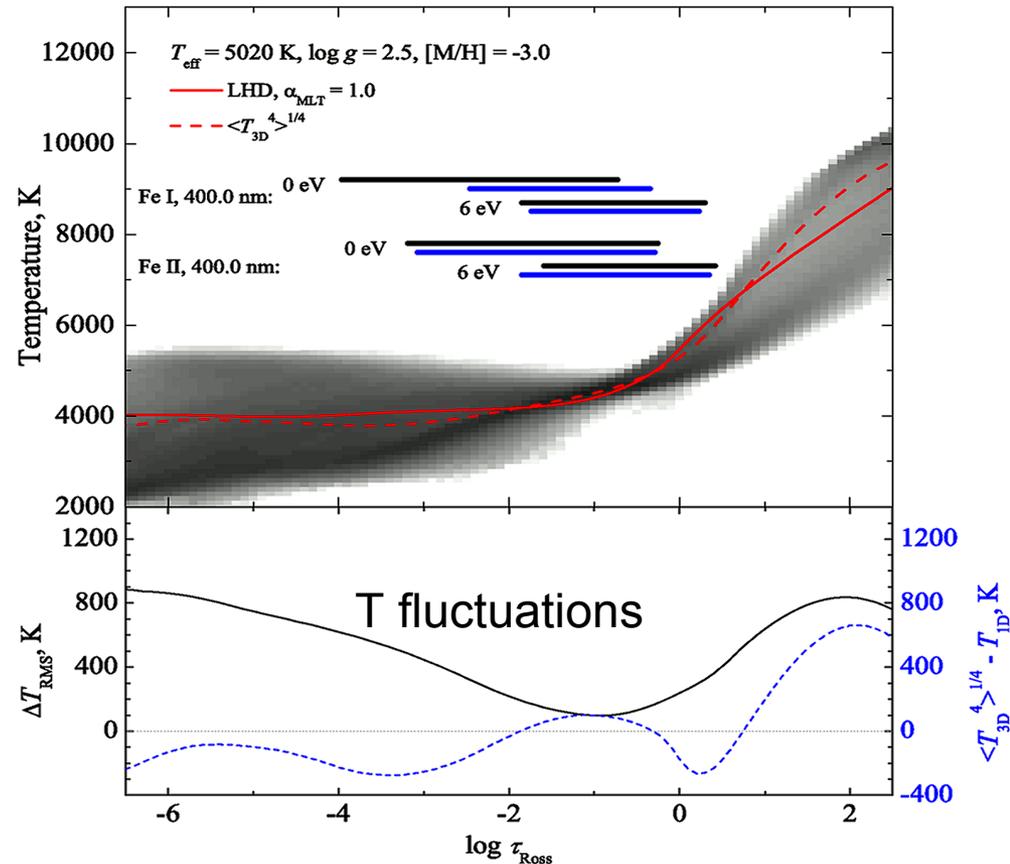
Convection in outer layers of cool stars affects vertical T profiles and creates horizontal T inhomogeneities.

Sveden Vacuum Solar Telescope



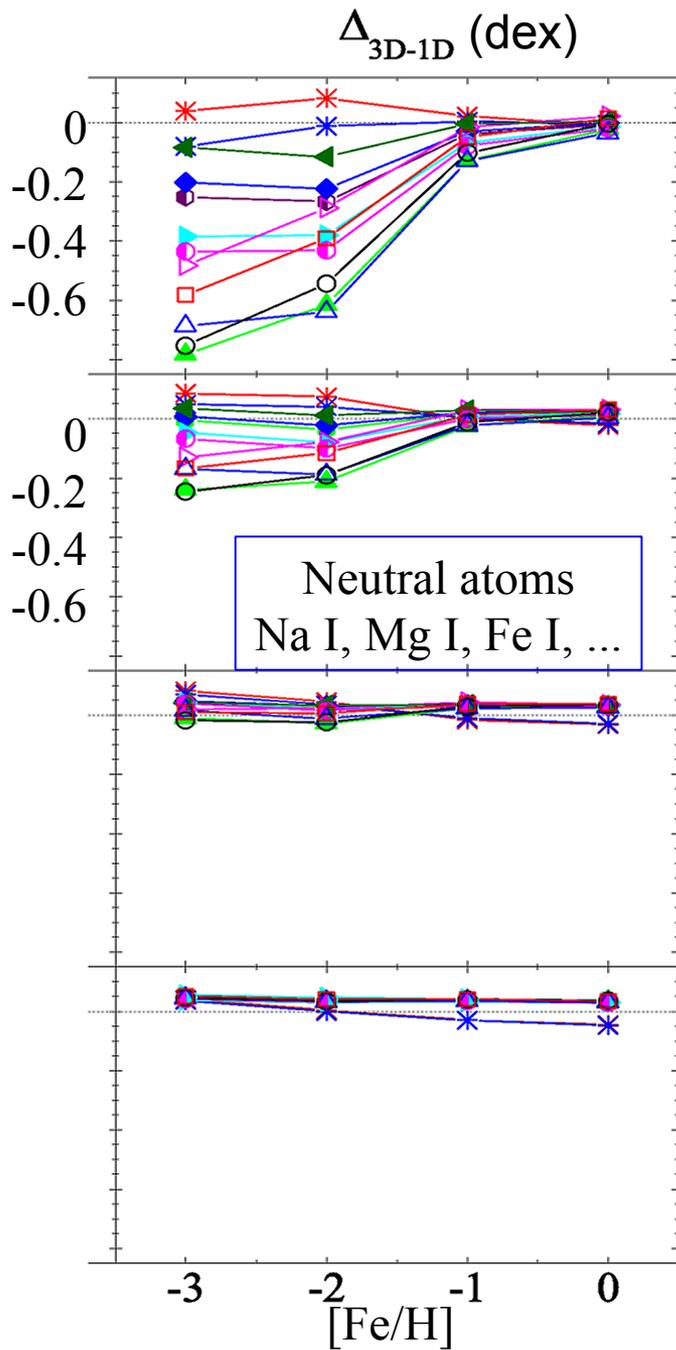
Solar granulation.

Size of area:  $\sim 65\,000$  km,  
granule:  $\sim 1\,000$  km.



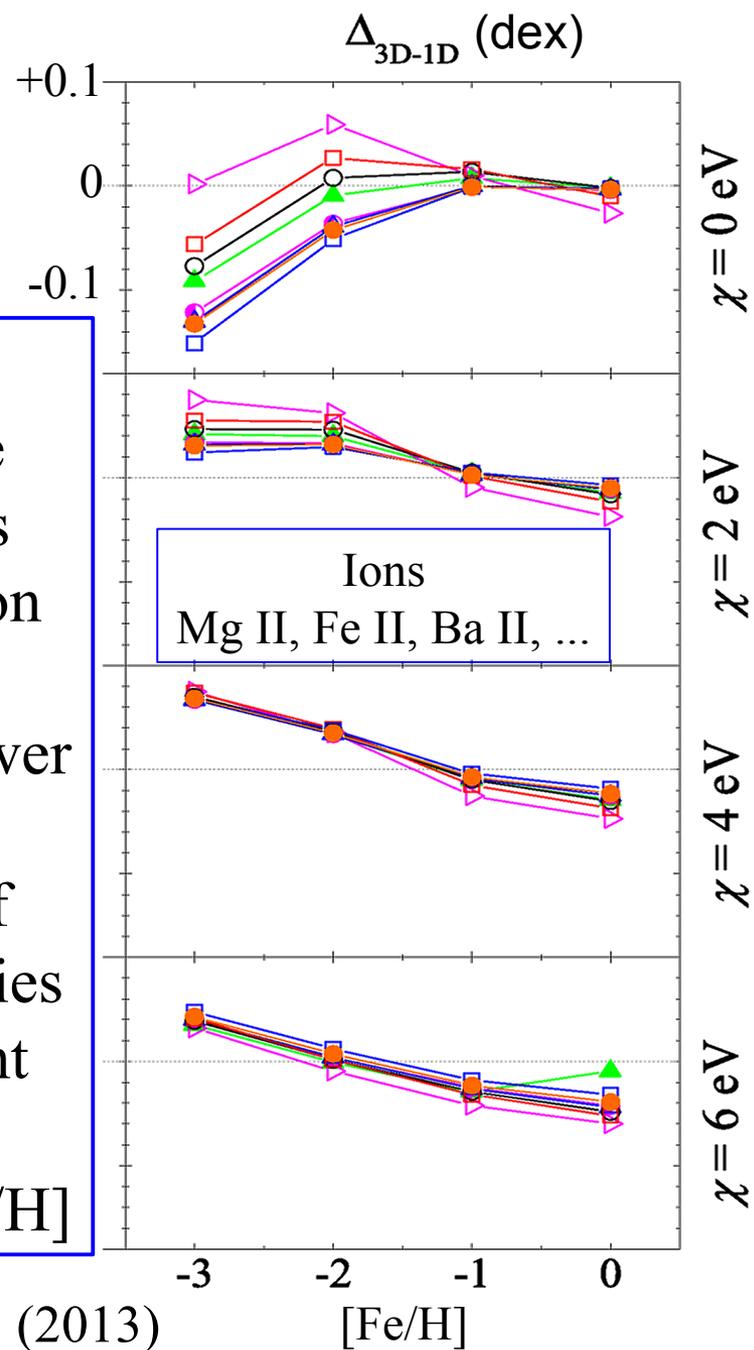
T profiles in 3D hydrodynamical CO<sup>5</sup>BOLD  
model atmosphere 5020/2.5/-3

*Dobrovolskas et al. (2013)*



3D-1D abundance corrections depending on excitation energy of lower level,  $\chi$ , for lines of various species in cool giant models of different  $[Fe/H]$

*Dobrovolskas et al. (2013)*



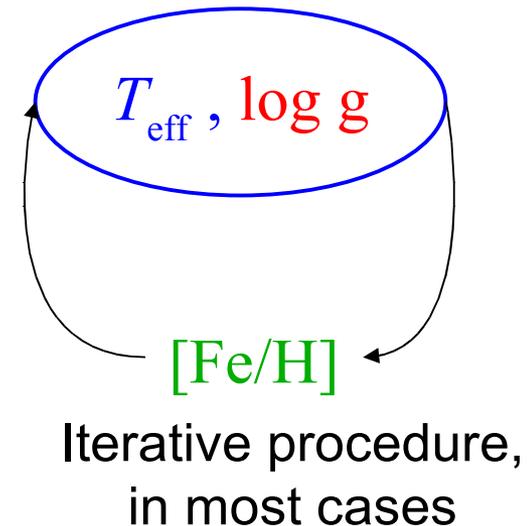
Before determination of chemical abundances  
one needs to determine  
atmospheric parameters  $T_{\text{eff}}$ ,  $\log g$ ,  $[\text{Fe}/\text{H}]$

- $T_{\text{eff}}$
- total flux and diameter measurements,  $f_{\text{obs}} = \sigma T_{\text{eff}}^4 \times \theta^2$ ,
  - photometric colors  $V-K$ ,  $b-y$ , etc.
  - spectroscopic methods: Balmer line profiles,  $EW$  ratios

### Surface gravity, $\log g$

- mass and radius measurements,  $g = G M/R^2$
  - distance,  $T_{\text{eff}}$ , mass,
  - $EW$  ratios (Fe I/Fe II, Ca I/Ca II, ...)
- Caution!* Departures from LTE for Fe I, Ca I.

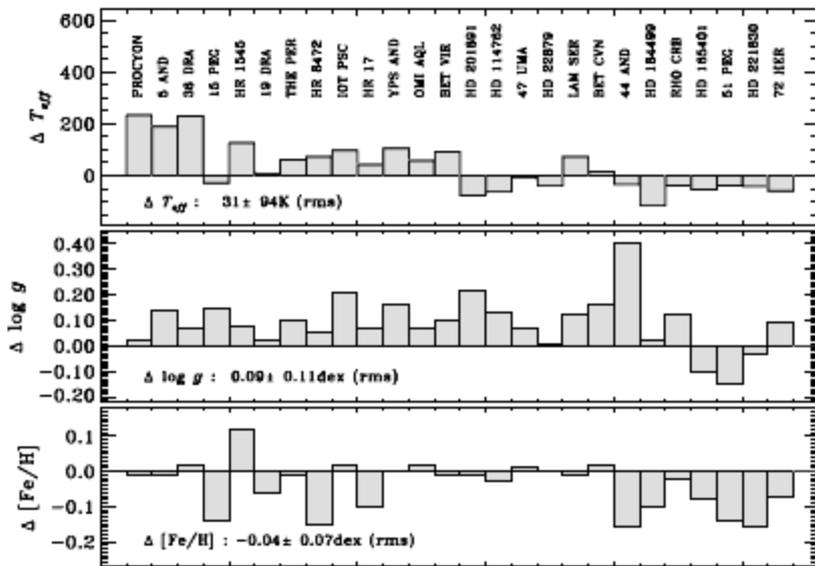
$[\text{Fe}/\text{H}]$  ▪ from lines of iron.



# Uncertainty in stellar parameters and effect on abundances

*Edvardsson et al. (1993)*

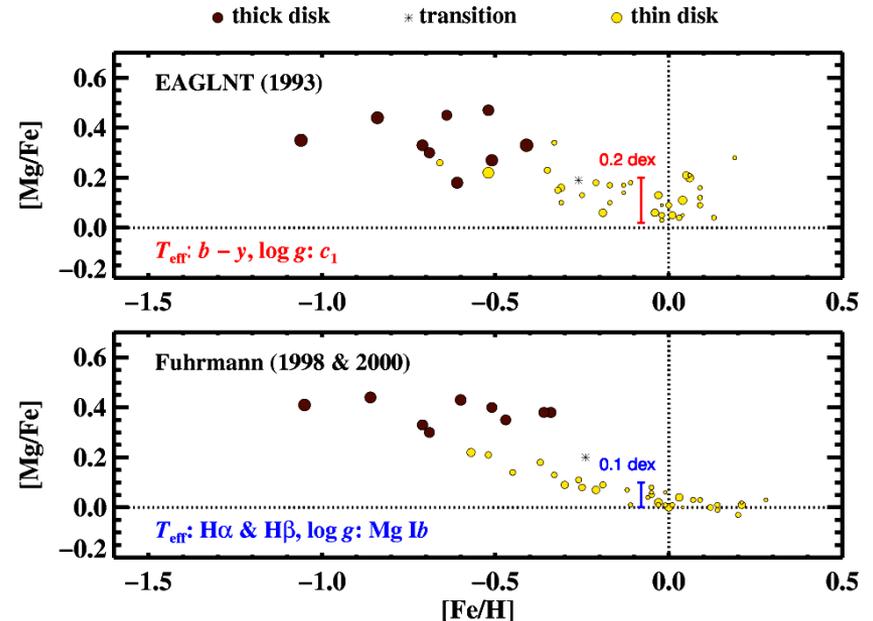
$T_{\text{eff}}$  from  $b-y$ ,  $\sigma(T_{\text{eff}}) = 100$  K  
 $g$  from  $c_1$ ,  $\sigma(\log g) = 0.1$



Differences in  $T_{\text{eff}}$ ,  $\log g$ ,  $[\text{Fe}/\text{H}]$  between two studies

*Fuhrmann (1998, 2000)*

$\text{H}\alpha$ ,  $\text{H}\beta$   
 $\text{Mg Ib}$



Spectroscopic stellar parameters lead to smaller scatter of  $[\text{Mg}/\text{Fe}]$

**HD 122563** is nearby ( $d = 237$  pc), well studied cool VMP giant:  
 $T_{\text{eff}} = 4600 \pm 60$  K (*Creevey et al.* 2012),  $\log g(\text{Hip}) = 1.60 \pm 0.07$ ,  
 $[\text{Fe}/\text{H}] = -2.56 \pm 0.07$  (*Mashonkina et al.* 2011)

### LTE abundances of heavy elements in HD 122563

based on Subaru/HDS spectra

	<i>Honda et al.</i> (2006)	<i>Mashonkina et al.</i> (2008)	
$T_{\text{eff}} =$	$4570 \pm 100$	$4600 \pm 60$	
$\log g =$	$1.1 \pm 0.3$ (Fe I/Fe II, LTE)	$1.5 \pm 0.2$ (Hipparcos)	
$[\text{Fe}/\text{H}] =$	$-2.77 \pm 0.19$	$-2.53 \pm 0.07$	
$\log \varepsilon(\text{Sr}) =$	$-0.12$	$0.07$	$\Delta \log \varepsilon = -0.19$
$\log \varepsilon(\text{Ba}) =$	$-1.65$	$-1.36$	$-0.29$
$\log \varepsilon(\text{Eu}) =$	$-2.77$	$-2.62$	$-0.15$

## Why is Ba/Eu important?

Heavy elements ( $Z > 30$ ) originate from

- ✓ slow ( $s$ -) process:
  - main component ( $A=90-208$ ), AGB stars of  $2-4 M_{\text{sun}}$ ,
  - weak component ( $A < 90$ ), He burning core of  $M > 10 M_{\text{sun}}$ ,
- ✓ rapid ( $r$ -) process: SNeII, neutron star mergers ??

### Solar System matter, Ba and Eu isotopes

	Lodders2009 (%)	$s$ -process (%)			Lodders2009 (%)	$s$ -process	
		A99	B11			A99	B11
$^{134}\text{Ba}$	2.4	100	100	$^{151}\text{Eu}$	47.8	6	6
$^{135}\text{Ba}$	6.6	26	30	$^{153}\text{Eu}$	52.2	5	6
$^{136}\text{Ba}$	7.9	100	100				
$^{137}\text{Ba}$	11.2	66	67				
$^{138}\text{Ba}$	71.7	86	94				
<b>Total Ba:</b>		<b>81</b>	<b>88.7</b>	<b>Total Eu</b>		<b>6</b>	<b>6</b>

Significant discrepancy!

81 to 89% of solar Ba are of  $s$ -process origin.

94% of solar Eu are of  $r$ -process origin.

- Solar system matter:  $\log \text{Ba/Eu} = 1.66$

- Solar system  $r$ -process (SSr):

$r$ -residuals = SS abundance –  $s$ -contribution

$$\log (\text{Ba/Eu})_r = 0.96 \text{ (A99),}$$

$$0.74 \text{ (B11).}$$

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**A99:**  $s$ -process calculations of *Arlandini et al.* (1999),

**B11:** *Bisterzo et al.* (2011).

- $r$ -process models

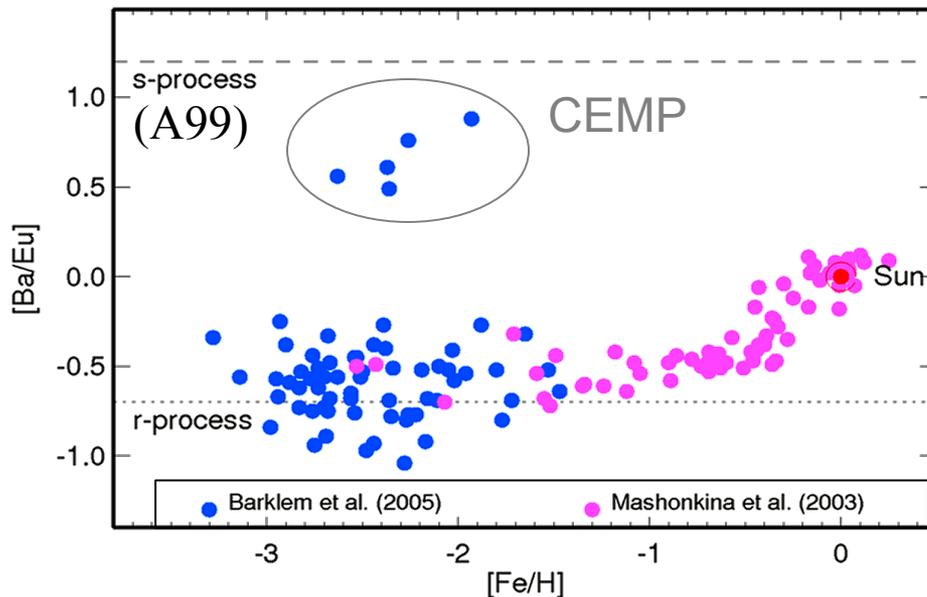
$\log (\text{Ba/Eu})_r \approx 1$ , WP approximation (*Kratz et al.* 2007),

0.8, HEW (*Farouqi et al.* 2010)

**Ba/Eu is sensitive to whether  $s$ - or  $r$ -process dominated heavy element production**

## Most MP stars are enriched in Eu

*Spite & Spite (1978),  
McWilliam (1998), Mashonkina & Gehren (2000),  
Barklem et al. (2005), Francois et al. (2007).*



- $-3.2 < [Fe/H] < -1$  stars form plateau at  $[Ba/Eu] \approx -0.6$ .

r-process dominated  
heavy element synthesis

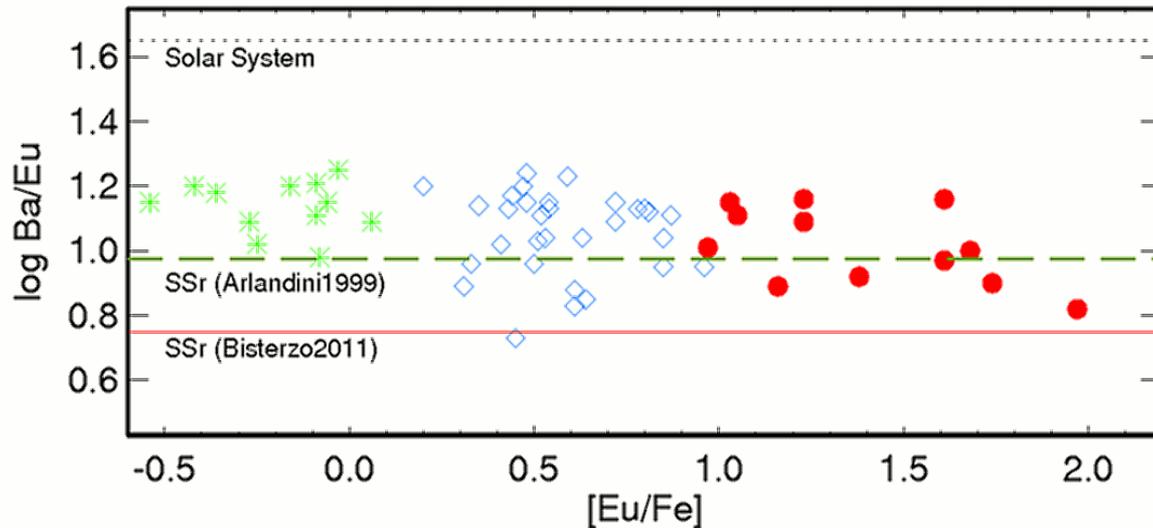
- $[Ba/Eu]$  grows at  $[Fe/H] > -1$ .

s-process  
contribution to Ba

## Why is Ba/Eu important?

Ba/Eu in  $[\text{Fe}/\text{H}] < -1.5$  stars with  $[\text{Ba}/\text{Eu}] < -0.4$

(based on literature data, in total, 14 sources)



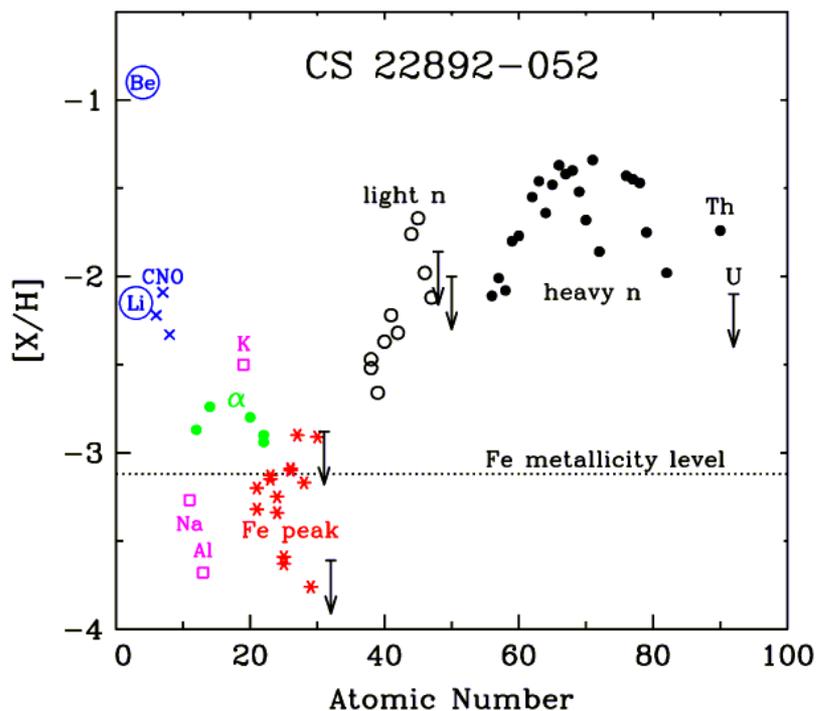
$\log \text{Ba}/\text{Eu} \approx 1$ ,  
independent of  $[\text{Eu}/\text{Fe}]$

- $[\text{Eu}/\text{Fe}] > 1$       r-II
  - ◇  $[\text{Eu}/\text{Fe}] = 0.3 - 1$       r-I
  - \*  $[\text{Eu}/\text{Fe}] < 0$       Eu-poor
- (Christlieb et al., 2004)

Is there problem with theoretical predictions  
or stellar observed Ba/Eu?

# r-II stars are best candidates for learning about r-process

- ✓ First discovery: CS 22892-052  
[Fe/H] = -3.1, [Eu/Fe] = 1.63.



30 elements from Sr to Th  
were measured

(*Snedden et al.* 1994, 1996, 2003)

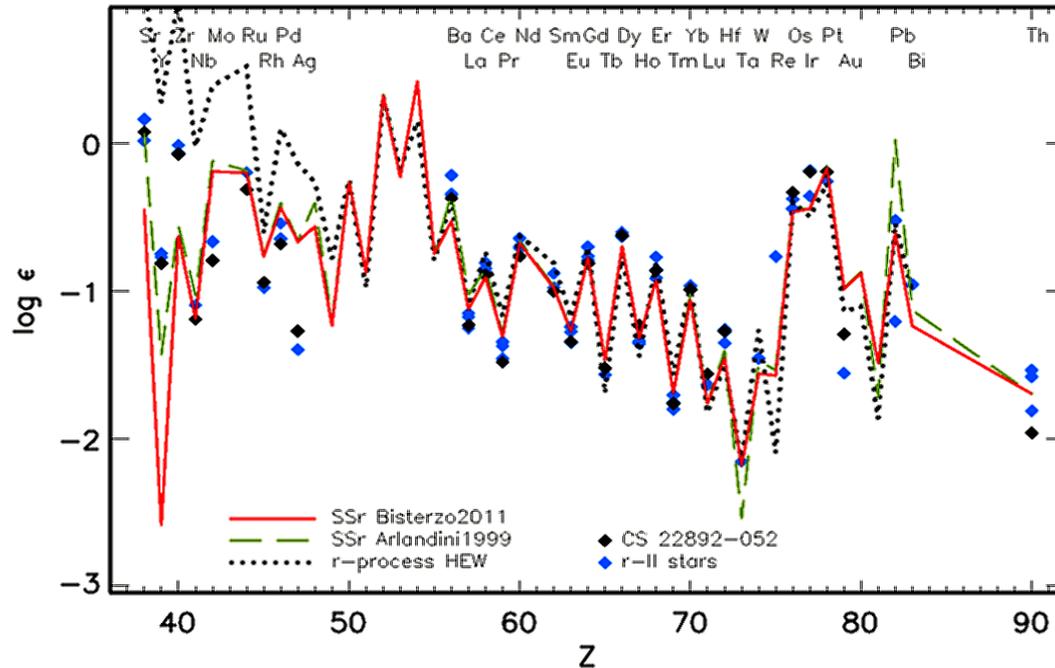
- ✓ CS 31082-001  
2001: detection of U (*Cayrel*, 2001)  
2013: 37 elements in Ge-U range  
(*Siqueira Mello et al.*, 2013)

- ✓ r-II: ~ 5 % of stars at [Fe/H] < -2.5  
(*Barklem et al.* 2005)

- ✓ 12 r-II stars were discovered:  
-3.4 ≤ [Fe/H] ≤ -2.8,  
[Eu/Fe] = 1.0 to 1.9

- ✓ n-capture element abundances of  
r-II stars are dominated by influence  
of single (few) r-process event(s).

# Element abundance patterns of r-II stars and SSr



CS 22892-052 (*Sneden03*)  
 CS 31082-001 (*Siqueira Mello13*)  
 HE 1523-091 (*Frebel07*)  
 HE 1219-0312 (*Hayek2009*),  


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 they all have  $[Eu/Fe] > 1.5$ .

- **r-II stars:** similar element patterns for Sr-Pt,  
 common origin of Sr-Pt in classical r-process.
- **SSr: Arlandini99 vs. Bisterzo11**  
 large differences in Sr, Y due to dominant contribution of s-process,  
 notable differences in Ba, La, Ta, Pb.
- **r-II stars vs. SSr:** similar element patterns for Ba-Hf,  
 universal r-process.

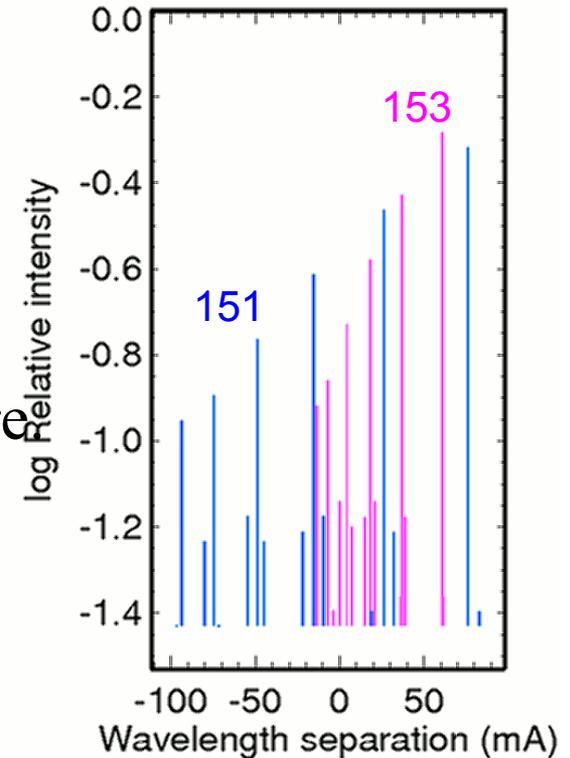
# Ba and Eu abundances of the r-II stars

need to be revised because

- different papers used different Ba isotope mixture,
- most papers did not take the departures from LTE for Ba II and Eu II into account.

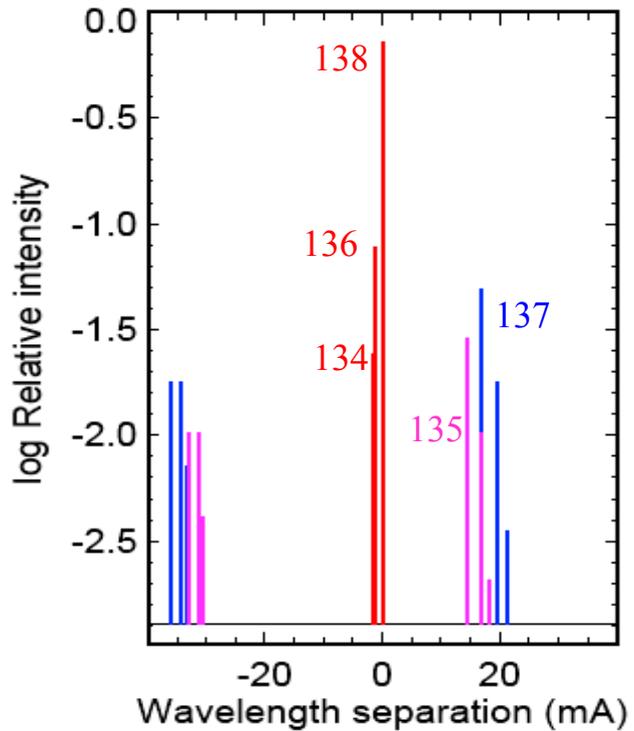
- In odd-atomic mass isotopes, nucleon-electron spin interactions lead to hyper-fine splitting (HFS) of the energy levels.
- Each line of Ba II and Eu II consists of isotopic (IS) and HFS components. They make the line broader resulting in larger absorbed energy.
- HFS and IS effects depend on isotope mixture
- Eu, two odd-A isotopes.
  - SS:  $^{151}\text{Eu}:^{153}\text{Eu} = 48:52$ ,
  - r-process:  $39:61$ .

Minor change in derived abundances between using two isotope mixtures.
- Ba: isotope mixture is different for SS matter and r-process.



Eu II 4129: isotopic and HFS components. Relative intensities correspond to  $^{151}\text{Eu}:^{153}\text{Eu} = 48:52$

# HFS and IS effects on derived Ba and Eu abundances

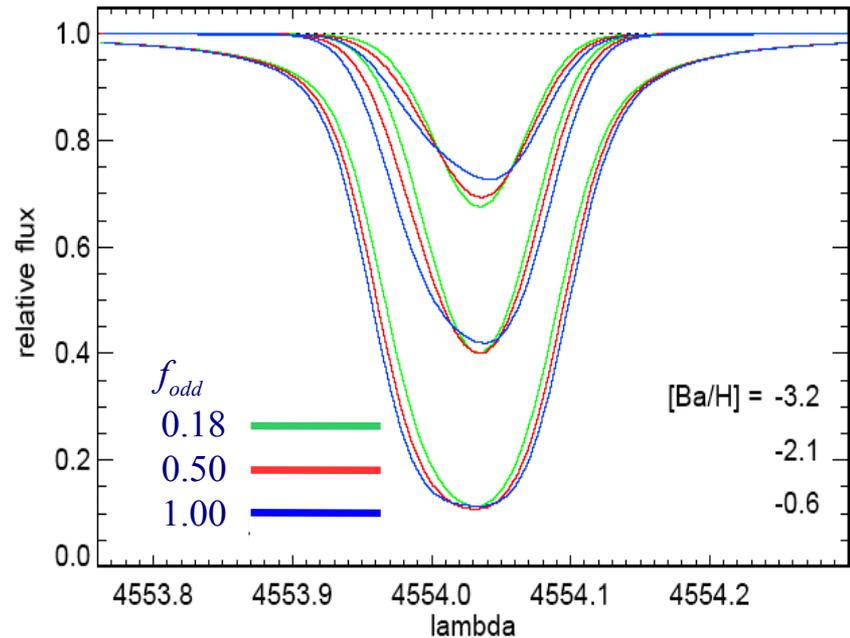


Ba II 4554 Å:

IS and HFS components.  
Relative intensities

correspond to  
SS Ba isotope mixture,

$$f_{odd} = 0.18.$$



- ✓ The greater  $f_{odd}$ , the stronger Ba II 4554 is. Ba abundances derived from resonance lines depend on adopted  $f_{odd}$
- ✓ HFS is negligible for subordinate lines of Ba II.

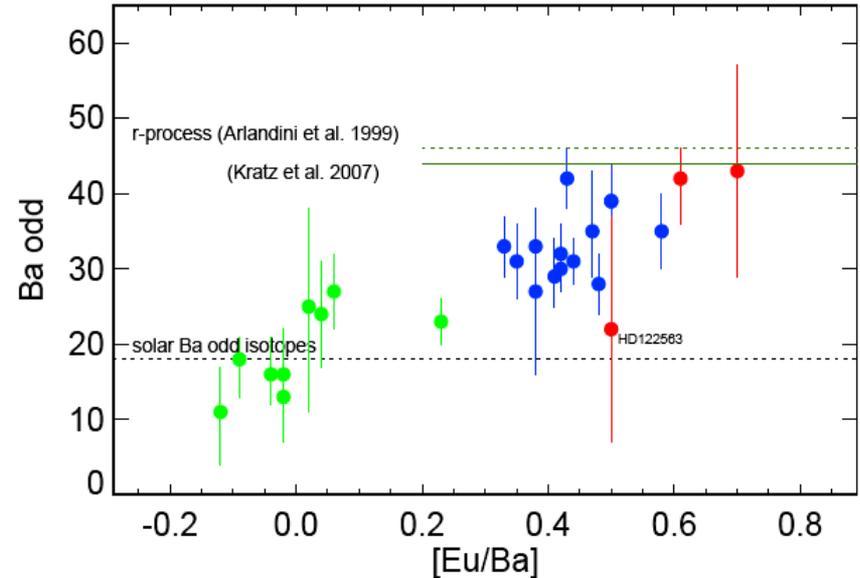
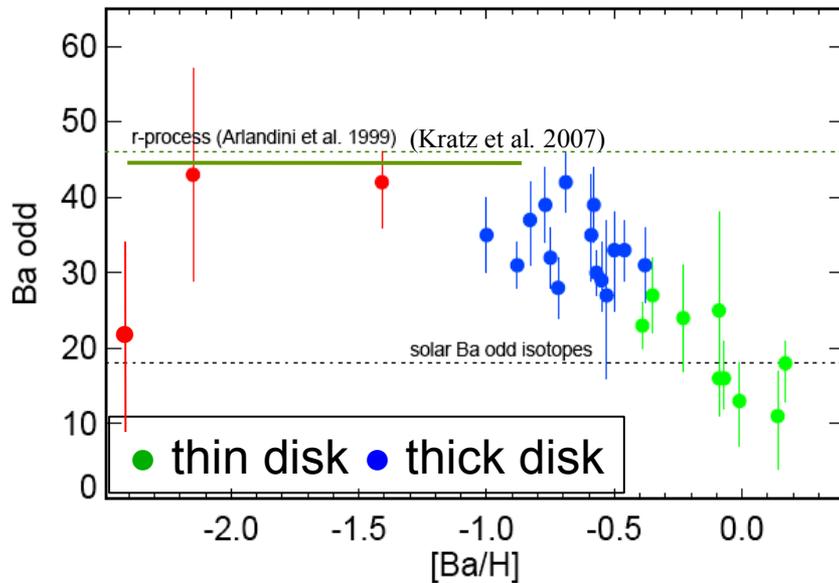
*Effect of using different Ba isotope mixtures  
for CS 22892-052, 4800/1.5/-3.1*

Mean non-LTE abundance (Ba II 4554, 4934 Å)	$f_{odd}$	
0.03	0.18	(Solar System)
$-0.18 \pm 0.01$	0.46	(A99)
$-0.28 \pm 0.03$	0.66	(B11)
-0.30	0.72	( <i>McWilliam</i> , 1998)
-0.20	0.52	( <i>Snedden et al.</i> 1996)
(Ba II subordinate lines)		
$-0.15 \pm 0.02$		

Ba abundances of Sneden star favor higher  $f_{odd} \approx 0.5$  than solar value.

Stellar  $f_{odd}$  can be evaluated from requirement  
 $\varepsilon(\text{Ba II resonance lines}) = \varepsilon(\text{Ba II subordinate lines})$

# Stellar fractional abundance of odd-A isotopes of Ba



thin disk }  $f_{odd}$  grows toward lower Ba and higher Eu/Ba  
 thick disk }

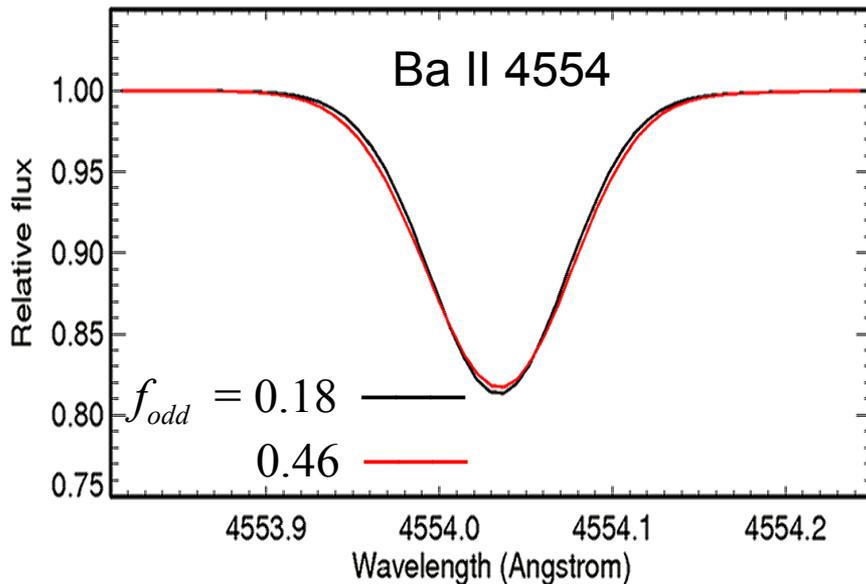
Halo stars:	[Fe/H]	$f_{odd}$	[Eu/Fe]	[Eu/Ba]	
HD 84937	-2.08	0.43	0.70	0.70	} r-I stars
HD 103095	-1.35	0.42	0.56	0.62	
HD 122563	-2.54	0.22	-0.51	0.50	Eu-poor

Different method is based on

*measuring the broadening of Ba II resonance lines,*

needs very high-quality stellar spectra:  $R > 100\,000$ ,  $S/N = 180$  to  $1100$ .

**HD 140283:**  $V = 7.2^m$ ,  $T_{\text{eff}} = 5750$  K,  $\log g = 3.7$ ,  $[\text{Fe}/\text{H}] = -2.5$



$f_{\text{odd}} = 0.08$  (Magain, 1995)

$0.30 \pm 0.21$  (Lambert &  
Allende Prieto 2002)

$0.15 \pm 0.12$  (Collet et al. 2009)

$0.02 \pm 0.06$  (Gallagher et al. 2010)

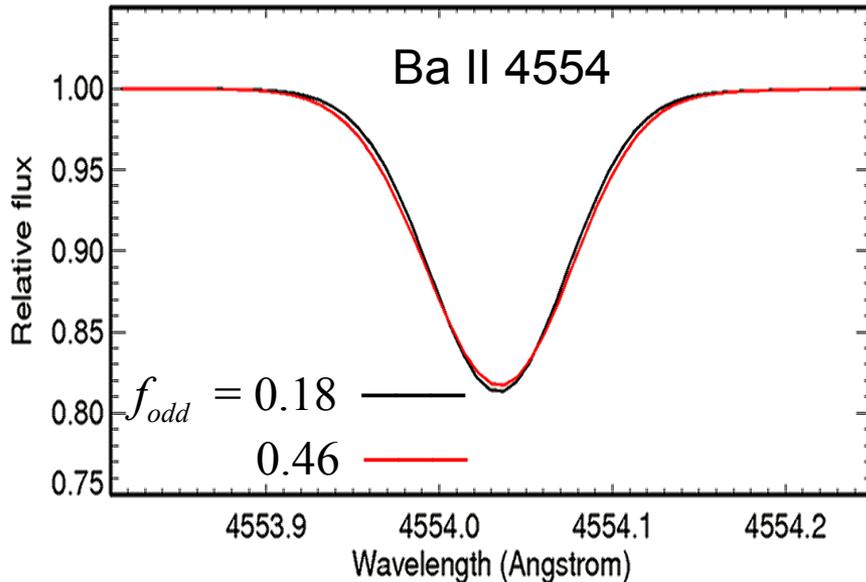
$f_{\text{odd}} = 0.18 \pm 0.08, 0.08 \pm 0.08, -0.02 \pm 0.09, -0.05 \pm 0.11, -0.12 \pm 0.07$   
for different 5 halo stars (Gallagher et al. 2012)

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$0.15 \pm 0.12$  (Caffau et al. 2011)

$0.02 \pm 0.06$  (Gallagher et al. 2012)

Pure s-process:

$f_{\text{odd}} = 0.11$

(Arlandini99)

$f_{\text{odd}} = 0.18 \pm 0.08, 0.08 \pm 0.08, -0.02 \pm 0.09, -0.05 \pm 0.11, -0.12 \pm 0.07$

for different 5 halo stars

(Gallagher et al. 2012)

## Problems and pitfalls of $f_{\text{odd}}$ determinations

### 1<sup>st</sup> approach: Ba II subordinate vs. resonance lines

Precise determination of abundance from individual lines:

- ✓ accurate  $T_{\text{eff}}$ ,  $\log g$ , microturbulence velocity,
- ✓ non-LTE effects,
- ✓ 3D effects on *abundances* are predicted to be small.

### 2<sup>nd</sup> approach: broadening of Ba II resonance lines

Precise measurement of line broadening:

- ✓ accurate star's rotation and macroturbulence velocity, instrumental profile,
- ✓ 3D effects on *line shape* can be significant.

We suspect that  $f_{odd}$  is related to the r-process abundances of the star.

All the r-process enhanced stars, HD103095, HD 84937, and the selected thick disk stars, with  $[Eu/Fe] = 0.24$  to  $0.70$ , reveal high  $f_{odd}$

HD122563 and HD 140283 are Eu-poor, with  $[Eu/Fe] = -0.51$  and  $< -0.2$ , and reveal low fractions of odd-A isotopes of Ba.

# Revision of Ba and Eu abundances of r-II stars

## Sources of observational data (spectra, EWs, LTE abundances):

*Snedden et al.* (1996); *Christlieb et al.* (2004); *Honda et al.* (2004);  
*Andrievsky et al.* (2009); *Aoki et al.* (2010); *Mashonkina et al.* (2010).

## Ba non-LTE abundances:

- Ba II subordinate lines that are nearly free of HFS  
(CS 22892-052, HE 1219-0312, HE 2327-5642, SDSS J2357),
- if only resonance lines are available, two  $f_{\text{odd}} = 0.46$  and  $0.66$   
(CS 22183-031, CS 29497-004),
- from *Andrievsky et al.* (2009)  
(CS 31082-001, CS 22953-003, subordinate and resonance lines,  $f_{\text{odd}} = 0.5$ ).

## Eu non-LTE abundances:

- 4 to 10 lines of Eu II in 8 stars.

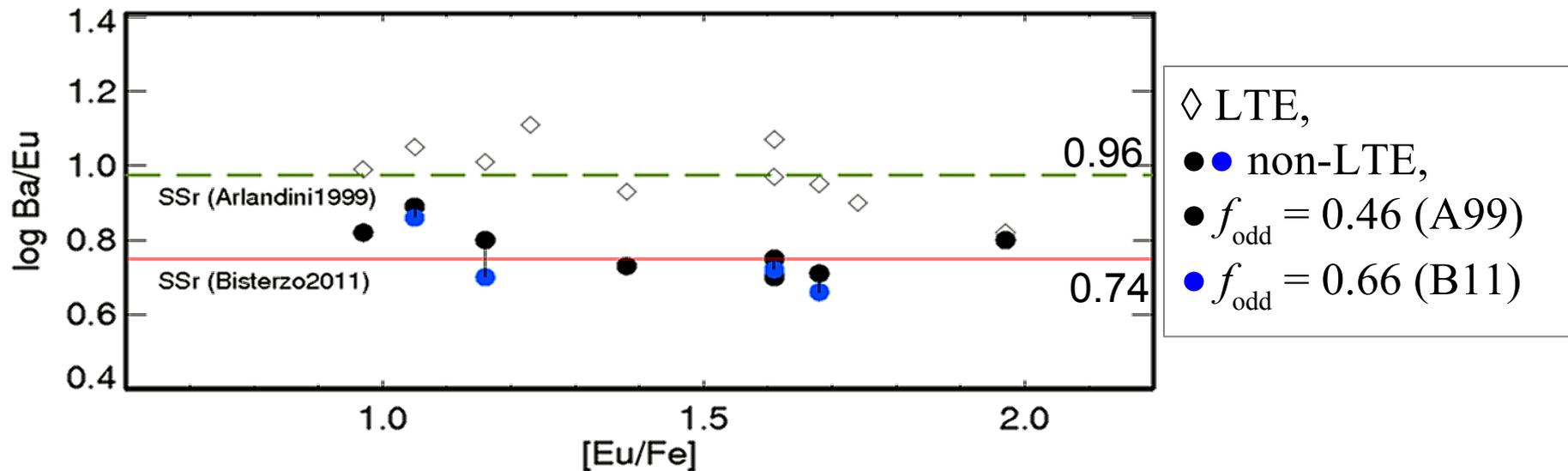
## Non-LTE effects depend on stellar parameters and the line

$$\Delta_{\text{NLTE}} = \log \varepsilon_{\text{NLTE}} - \log \varepsilon_{\text{LTE}}$$

$T_{\text{eff}}/\log g/[\text{Fe}/\text{H}]/[\text{Ba}/\text{Fe}]$	Ba II 4554	5853	6497	[Eu/Fe]	Eu II 4129
4800/1.5/-3/ 1.1	-0.13	-0.14	-0.35	1.8	0.06
4800/1.5/-3/ 0.7	-0.14	-0.02	-0.22	1.6	0.08
5050/2.3/-3/ 0.7	-0.15	0.02	-0.11	1.5	0.10
5010/4.8/-3/ 0.7	-0.01	0.01	0.01	1.5	0.03

- ✓ r-II stars are mostly VMP cool giants.  
Non-LTE leads to *lower* Ba, but *higher* Eu abundance.
- ✓ Exception is VMP dwarf with  $[\text{Eu}/\text{Fe}] = 1.9$  (Aoki et al. 2010).  
Non-LTE effects are minor.

# Ba/Eu of r-II stars



LTE, mean  $\log \text{Ba/Eu} = 0.99$  (10 stars)  
 non-LTE,  $f_{\text{odd}} = 0.46$  0.78 (8 stars)  
 non-LTE,  $f_{\text{odd}} = 0.66$  0.75

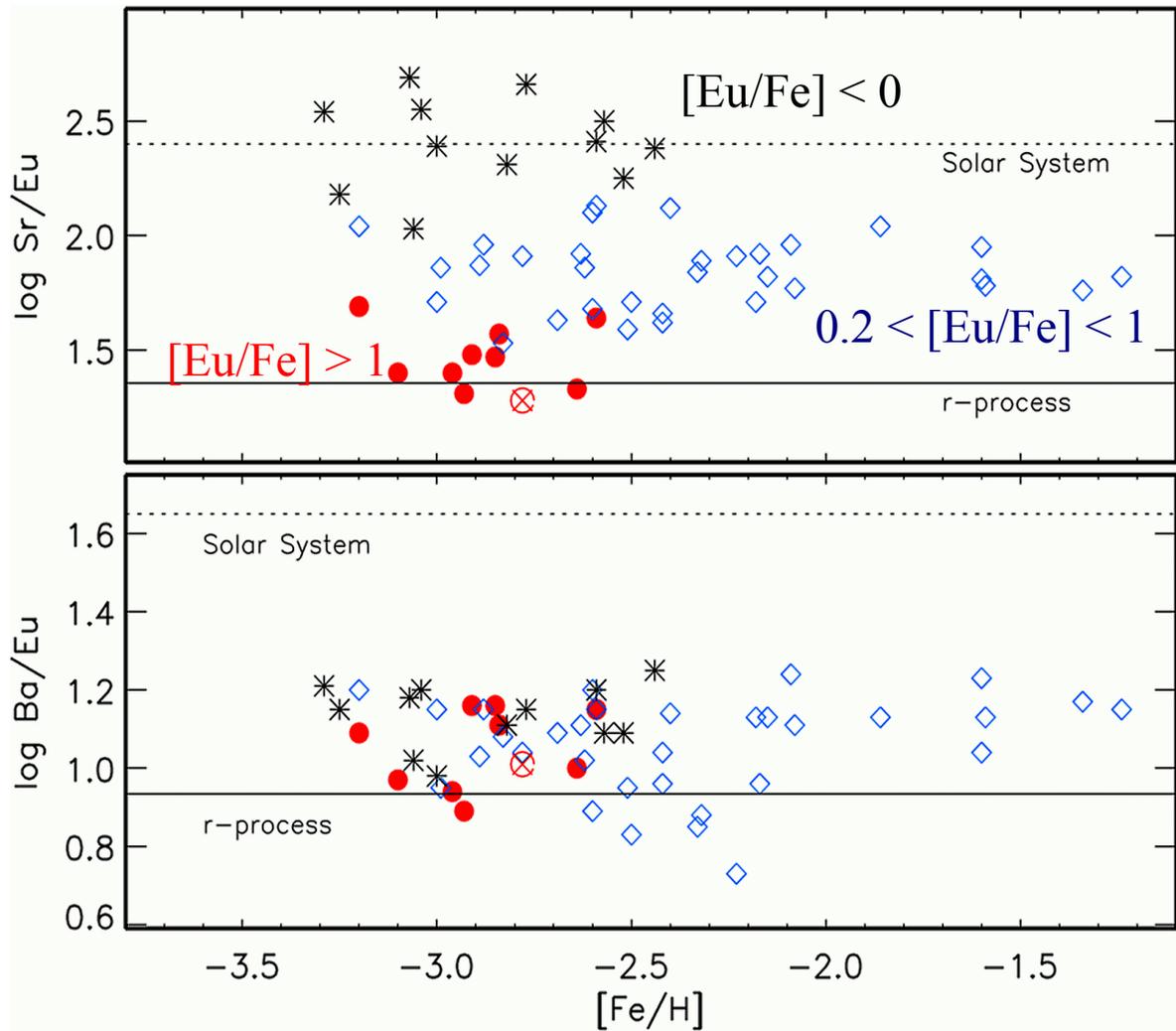
For 4 stars,  
 Ba abundances  
 depend on used  
 Ba isotope mixture.

Ba/Eu non-LTE ratios of the r-II stars support

- ✓ updated solar r-process  $\log (\text{Ba/Eu})_r = 0.74$  (*Bisterzo et al. 2011*)
- ✓ HEW r-process model  $\log (\text{Ba/Eu})_r = 0.8$  (*Farouqi et al. 2010*)

## Concluding remarks

- ◆ When deriving element abundances, take care of high-quality star's spectrum, accurate stellar parameters, adequate atmosphere and line-formation modelling.
- ◆ Revised Ba/Eu abundance ratios of the r-II stars favor chemical evolution calculations of *Bisterzo et al.* (2011) and HEW r-process model by *Farouqi et al.* (2010).
- ◆ For constraining r-process models, it would be important to determine fraction of the odd isotopes of Ba in the r-II stars.



Sr/Eu

and

Ba/Eu  
in metal-poor stars

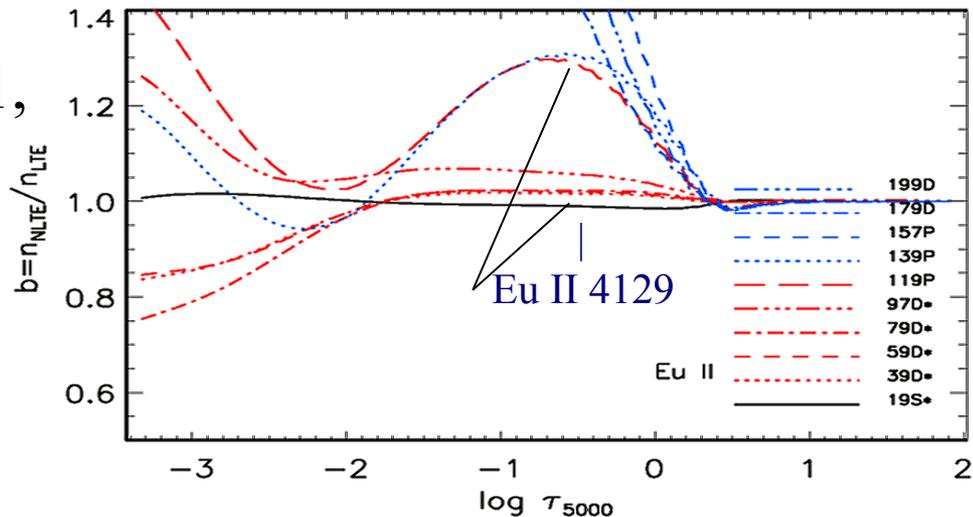
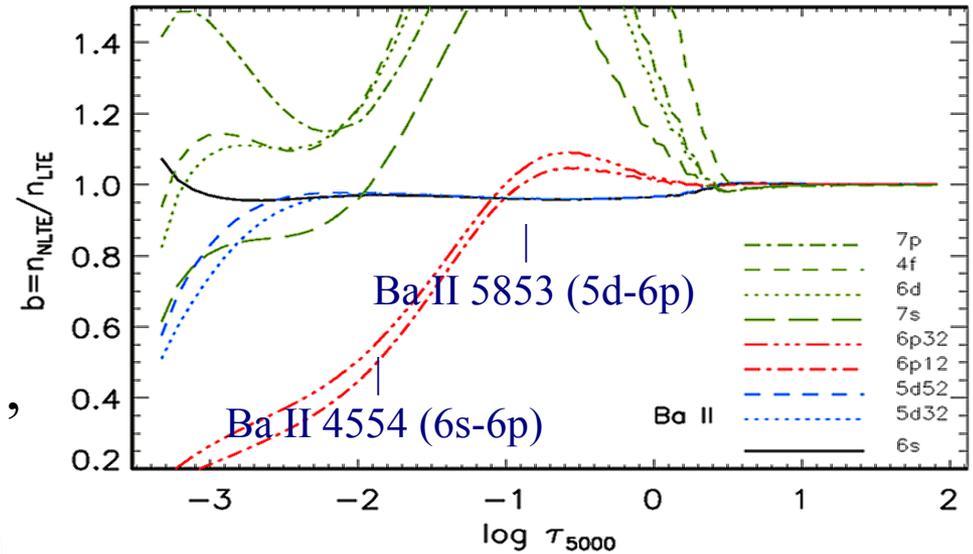
*Mashonkina et al. (2010)*

## Departure coefficients

$$b = n_{\text{NLTE}}/n_{\text{LTE}}$$

for Ba II and Eu II  
in 4800/1.5/-3 model

- Ba II 4554:  $b(6s) \approx 1$ ,  $b(6p) < 1$ ,  
line is strengthened, with  
non-LTE abundance correction  
 $\Delta_{\text{NLTE}} = -0.14$  dex.
- Ba II 5853:  $b(5d) \approx 1$ ,  $b(6p) \approx 1$ ,  
 $\Delta_{\text{NLTE}} = -0.03$  dex.
- Eu II 4129:  $b_{\text{low}} \approx 1$ ,  $b_{\text{up}} > 1$   
line is weakened,  
 $\Delta_{\text{NLTE}} = +0.10$  dex.



## Method of calculations

- Non-LTE populations for Ba II and Eu II:
  - model atoms and atomic data from *Mashonkina et al.* (1999),  
*Mashonkina* (2000, updated)
  - code DETAIL by *Butler & Giddings* (1985)  
with updated opacity package.
- Spectral line synthesis: code SIU by *Reetz* (1991).
- Model atmospheres: MARCS (*Gustafsson et al.* 2008)